Functional and Logic Programming cpsc 370 Fall 2018 Currying Questions—Monday, September 17 2018

Questions

1. Consider the relations

(2)

- $A = \{ (\bot, \{ (\diamondsuit, \pi), (\clubsuit, \pi) \}), (\top, \{ (\diamondsuit, \pi), (\clubsuit, 3) \}) \}$
- $B = \{ (\bot, \{ (\clubsuit, \pi), (\clubsuit, \pi) \}), (\top, \{ (\clubsuit, 3) \}) \}$
- $C = \{ ((3, \clubsuit), \top), ((3, \bigstar), \bot), ((\pi, \clubsuit), \bot), ((\pi, \bigstar), \bot) \}$
- (a) Which of the above are functions? Why?
- (b) Are either sets *A* or *B* Curried functions? Why or why not?
- (c) The set *C* is a function. What is its Curried form?
- Sometimes it is useful to consider subsets as defined by a function on the larger set that returns true if and only if an element is a member of a subset. Let 2 = { ⊤, ⊥ } be the set containing true (⊤) and false (⊥). The observation about subsets means that the power set of *S*, *P*(*S*) can be thought of as a set of functions: *P*(*S*) ≡ 2^{*S*}.

Use this and Currying to explain why a relation *r* on $S \times T$ can be thought of as a function \hat{r} from *S* to $\mathcal{P}(T)$.