

Dijkstra's Dutch Flag Problem

Goals:

The goals of this laboratory exercise are three-fold:

- To practise using loop-invariants.
 - To better understand the partition algorithm.
 - To gain confidence in interfacing with libraries supplied by someone else.
-

Due Date:

This assignment is in two parts.

- Part I is due *Wednesday, 03 November* by the beginning of class.
 - Part II is due *Wednesday, 10 November* by the beginning of class.
-

Utilities

Your goal for this part of the assignment is to write a `Utilities` class that contains several small algorithms for working with a generic array. The interface is shown in Figure 1 on page 5.

With the exception of the `swap` method, each of these algorithms contains one or more loops. Write your code to contain a comment that describes the loop invariant, as shown in the sample `shuffle` algorithm.

There are four `isSorted` algorithms for determining if a section $[\ell, r)$ of an array `data` is sorted with respect to a comparator `c`. If $[\ell, r)$ is not supplied, it should be taken to be $[0, \text{data.length})$. If the comparator `c` is not supplied, it should be taken to be `Comparator.naturalOrder()`. Three of these algorithms should just call a different flavour of the algorithm. The fourth should document its loop invariant(s).

Finally, there is a `partition` algorithm. The intent is as follows: after executing

```
int m = partition(data, ell, arr, p);
```

the following should be true:

1. for $i \in [0, \ell)$, `data[i]` should be unchanged.
2. for $i \in [\ell, m)$, `p.test(data[i])` should be false.
3. for $i \in [m, r)$, `p.test(data[i])` should be true.

4. for $i \in [r, n)$, `data[i]` should be unchanged.

where $\ell = \text{ell}$, $r = \text{arr}$, and $n = \text{data.length}$.

- ⇒ Explain why this partition algorithm is slightly different from the quick sort partition algorithm.
- ⇒ Submit your `Utilities.java` file via blackboard.
- ⇒ This part is due by Wednesday, 03 November.

The Dutch Flag problem

The Dutch flag problem is due to Edsger Dijkstra, and illustrates the value of carefully thinking through loop invariants.

The problem goes as follows. You are given an array filled with n red, white, and blue objects; and you are to sort the array so that the red objects are to the left, and the blue ones to the right.¹ In general, sorting requires $\Omega(n \log n)$ average time, but in this particular case, because there are only three possible kinds of objects, you can achieve $\Theta(n)$ worst-case time.

Write two algorithms to solve the Dutch flag problem.

1. The first algorithm should use a single for-loop. Before coding this algorithm, draw a loop invariant that show where four regions—the red region, the white region, the blue region, and the unknown region—lie, and what variables describe the edges of the regions. Include the loop invariant, either directly in the code, or in separate documentation.
2. The second variant should contain no loops, and two calls to `Utilities.partition` (See the note below about λ -expression for help with using `partition` on `RedWhiteBlue` objects.)

Write your algorithms to be compatible with the `RedWhiteBlue` class shown in Figure 2 on page 6. An implementation of this class will be given to you as a `.jar` file on the blackboard site (see “Using `.jar` files” below).

Test both of your algorithms by

1. showing that they correctly sort a random array (using `Utilities.isSorted`), and
2. showing that the running time is linearly proportional to the problem size (by plotting, as in previous labs).

- ⇒ Submit your `*.java` for your `Utilities` class, your `Stopwatch` class, your two algorithms for sorting, and your testing code.
- ⇒ Submit your test data.
- ⇒ This part is due by Wednesday, 10 November.

¹To be truly Dutch, the red ones should be at the top, and the blue ones at the bottom. Red on the outside and blue on the inside is the French flag.

Using .jar files

Exactly how to use .jar files depends on how you compile and run JAVA.

If you use basic command line compilation, something like

```

UNIX
javac -cp .:RBW.jar *.java
java -cp .:RBW.jar Main

```

or²

```

WINDOWS
javac -cp .;RBW.jar *.java
java -cp .;RBW.jar Main

```

should work (assuming that `public static void main(...)` is contained in `Main.java`).

λ -expressions, or how to make a Predicate

In order to separate the red objects from the non-red objects in an array of `RedWhiteBlue` objects using `Utilities.partition`, we need to create an object that satisfies the interface `java.util.function.Predicate`. Here is a sequence of decreasingly painful ways to do so:

1. create a named class implementing `Predicate`, then create an object:

```

1 private static class RedPredicate implements Predicate<RedWhiteBlue>
2 {
3     public boolean test(RedWhiteBlue obj) { return obj.isRed() ; }
4 }
5 // ...
6 Utilities.partition(data, new RedPredicate()) ;

```

2. create an object of an anonymous class implementing `Predicate`:

```

1 var redPredicate = new Predicate<RedWhiteBlue> ()
2 {
3     public boolean test(RedWhiteBlue obj) { return obj.isRed() ; }
4 } ;
5 Utilities.partition(data, redPredicate) ;

```

3. create an explicit λ -expression as follows

```

1 Utilities.partition(data, (obj)->{ return obj.isRed() ; }) ;

```

4. create an explicit λ -expression, but use some shortcuts

```

1 Utilities.partition(data, obj->obj.isRed() ) ;

```

5. Use a `::` expression:

```

1 Utilities.partition(data, RedWhiteBlue::isRed ) ;

```

More information about JAVA λ expressions can be found at:

²Thaks to KT for reminding me that WINDOWS has a different path syntax

- <https://docs.oracle.com/javase/tutorial/java/java00/lambdaexpressions.html>
- <http://tutorials.jenkov.com/java/lambda-expressions.html#var-parameter-types-java-11>
- <https://www.baeldung.com/java-8-lambda-expressions-tips>

```
import java.util.function.Predicate ;           1
import java.util.Comparator ;                 2

public class Utilities                          3
{
    // a classic                                4
    public static <E> void swap(E [] data, int i, int j)    {...} 5
    // tests for sortedness                      6
    public static <E extends Comparable<? super E>>
    boolean isSorted(E [] data)                {...} 7
    public static <E>
    boolean isSorted(E [] data, Comparator<E> c)    {...} 8
    public static <E extends Comparable<? super E>>
    boolean isSorted(E [] data, int i, int j)    {...} 9
    public static <E>
    boolean isSorted(E [] data, int i, int j, Comparator<E> c) {...} 10
    // a general purpose partition algorithm      11
    public static <E>
    int partition(E [] data, int ell, int arr, Predicate<E> p) {...} 12
    // a sample algorithm, with loop invariant    13
    public static <E> void shuffle(java.util.Random rnd, E [] data) 14
    {
        final int n = data.length ;             15
        for(int i=n;i>1;--i)                   16
        {
            // Loop Invariant:                  17
            //   The n-i rightmost elements are randomly selected    18
            //   with equal probabilities from the initial array.     19
            //   The range [0,i) contains the elements that have not  20
            //   yet been selected.                21
            swap(data,i-1,rnd.nextInt(i)) ;    22
        }
    }
}
```

Figure 1: Utilities class declaration

```
public class RedWhiteBlue implements Comparable<RedWhiteBlue> 1
{ 2
    // ... implementation details 3

    public int compareTo(RedWhiteBlue that) { ... } 4
    // Red < White < Blue 5
    6

    @Override 7
    public String toString () { ... } 8
    9

    // Queries to determine the color of an object. 10
    public boolean isRed () { /* ... */; } 11
    public boolean isWhite() { /* ... */; } 12
    public boolean isBlue () { /* ... */; } 13
    // for a given object, exactly one of isRed, isWhite or 14
    // is isBlue is true 15
    16

    /* ===== 17
    * static methods to get RedWhiteBlue objects 18
    */ 19
    public static RedWhiteBlue getRed () { /* ... */ } 20
    public static RedWhiteBlue getWhite () { /* ... */ } 21
    public static RedWhiteBlue getBlue () { /* ... */ } 22
    // getWhite().isWhite() is true, and so on ... 23
    24
} 25
26
27
```

Figure 2: RedWhiteBlue class declaration